

DE LA RECHERCHE À L'INDUSTRIE



## Performance modeling of an industrial hydrocode on recent multicore processors

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- 1 Goals and target application
- 2 Performance model: the Roofline
- 3 Application of the Roofline model to the current solver
- 4 The ECM model
- 5 Conclusions

Build a solver for compressible fluid dynamics (Euler equations) which will run efficiently on current and future computers

## Understand HPC properties of the reference numerical method

- Analyze and understand the current solver performance

## Improve the current solver to its limits

- Understand current processor micro-architectures
- Optimize the solver implementation for current processors micro-architectures
- Estimate the maximal achievable performance for this solver

## Going further

- Predict performance on other and future architectures
- Design a solver based on a more efficient algorithm

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⇒ Building performance model

## 1 - Lagrangian step

Compute evolution of hydrodynamic quantities on a mesh moving at material velocity

## 2 - Remap step

Remap / interpolation from distorted mesh to fixed initial one

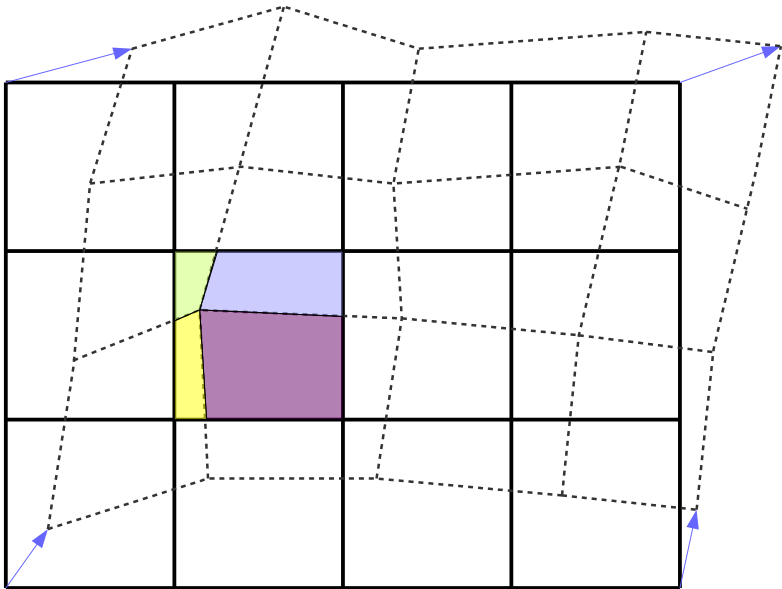


Figure: Sketch of Lagrange-Remap methods

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## Definition

Build and use simple abstraction to estimate execution time of a chosen algorithm on a given computing architecture  
⇒ Understanding the performance behavior of a code

## Interests

- Define how efficiently a computer is used (current usage vs machine peak)
- Predict / extrapolate performance behavior on others architectures
- Provide optimization hints

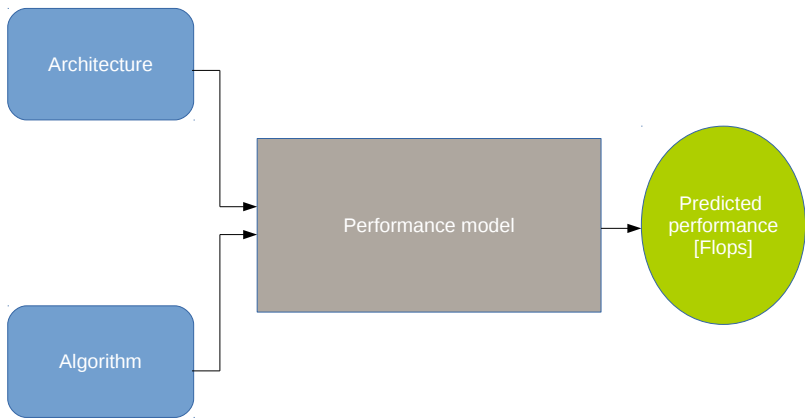


Figure: Input / output of a performance model

## Architecture

- **Bandwidth:**  
Data transfers rate from memory to computing units[GBytes/s]
- **Peak:**  
Absolute maximum performance of a computer[GFlops]

## Algorithm

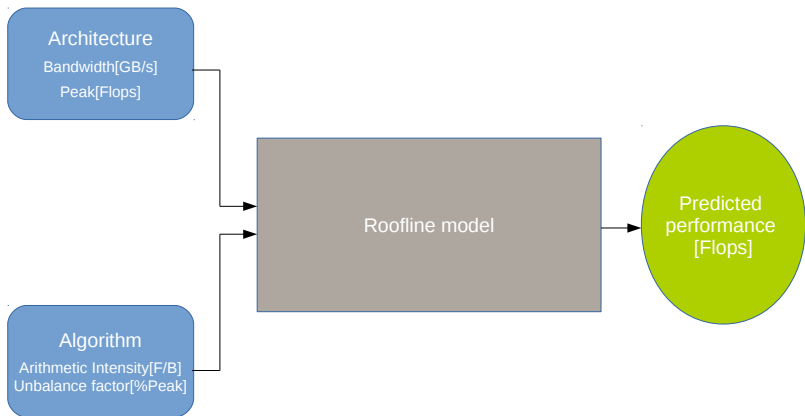
- **Arithmetic Intensity (AI):**  
$$AI := \frac{\text{number of operation}}{\text{quantity of data transfered}} \text{ [Flops/Byte]}$$
- **Unbalance factor (instruction mix):**  
Reduction performance factor due to not perfect matching between algorithm and architecture [%peak]

## (ideal) Roofline model

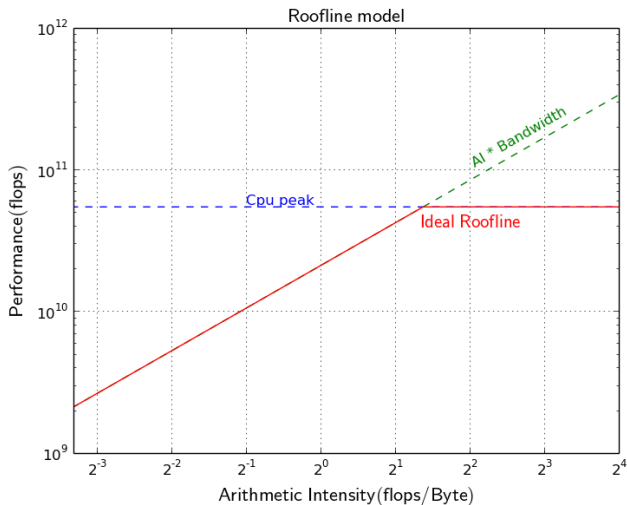
$$\begin{aligned} \text{Perf(ideal)} &= f(\text{Peak}, \text{bandwidth}, \text{AI}) \\ &:= \min(\text{Peak}, \text{bandwidth} \times \text{AI}) \end{aligned}$$

## (effective) Roofline model

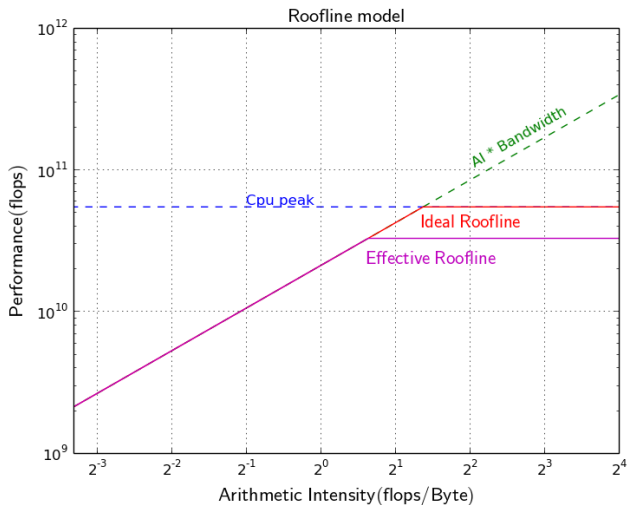
$$\begin{aligned} \text{Perf(effective)} &= f(\text{Peak}, \text{bandwidth}, \text{AI}, \text{unbalance factor}) \\ &:= \min(\text{Peak} \times \text{unbalance factor}, \text{Bwd} \times \text{AI}) \end{aligned}$$



# Roofline: graphical representation



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# Dataflow diagram of the remap step

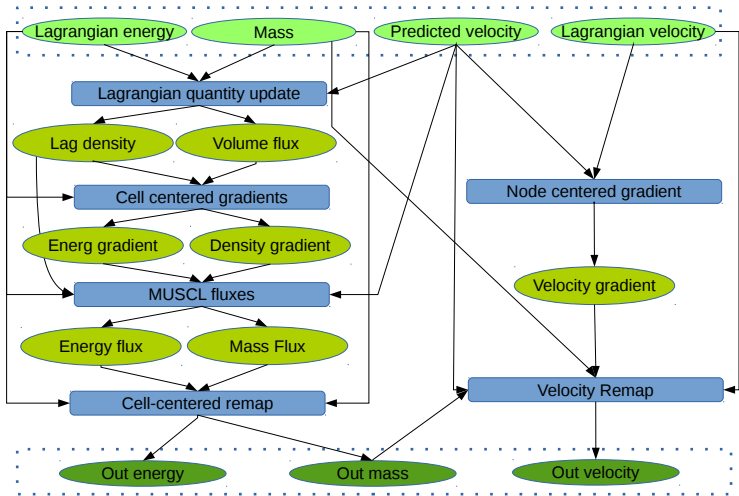
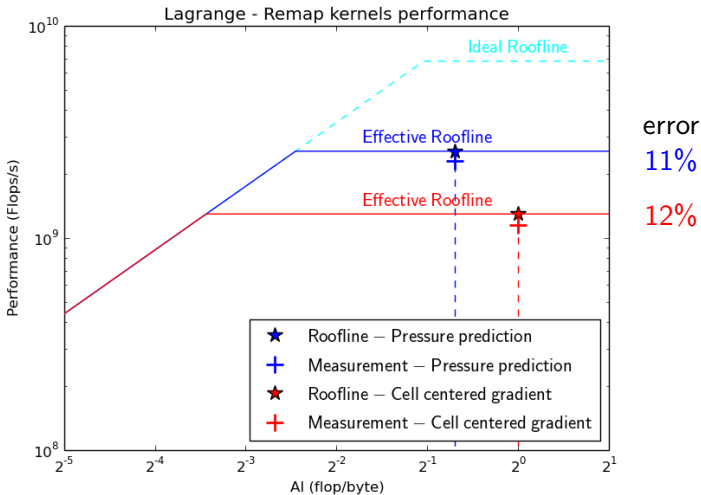
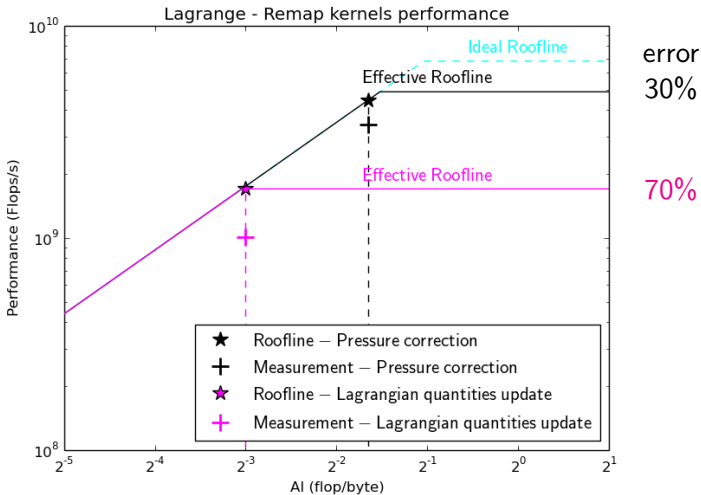


Figure: Dataflow diagram of the remap step

# Roofline model vs measured performance



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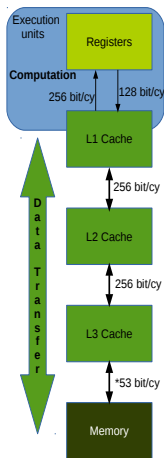
**ECM** (Execution Cache Memory model):  
refinement of the Roofline model by introducing  
data transfers through caches

Metrics: time [cycles / cache line update]

- Time for pure computation (assuming data are in L1 Cache)
- Times for data transfers through the different cache levels L1-L2, L2-L3, L3-Ram

Main hypotheses

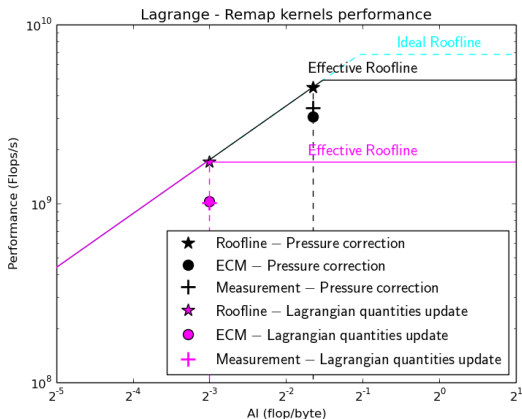
- Computations and data transfers may overlap
- Data transfers do not overlap



Haswell AVX kernels	ECM	measurements	error
<i>Lagrange kernels</i>			
Pressure prediction	168	173	3%
Pressure correction	80	78	3%
Velocity update	89	65	8%
<i>Remap kernels</i>			
Lag. q. update	57	58	2%
Cell centered gradient	168	170	1%
MUSCL Flux	44	42	5%
Cell centered remap	76	65	17%
Node centered gradient	168	170	1%
Velocity remap	30	25	17%

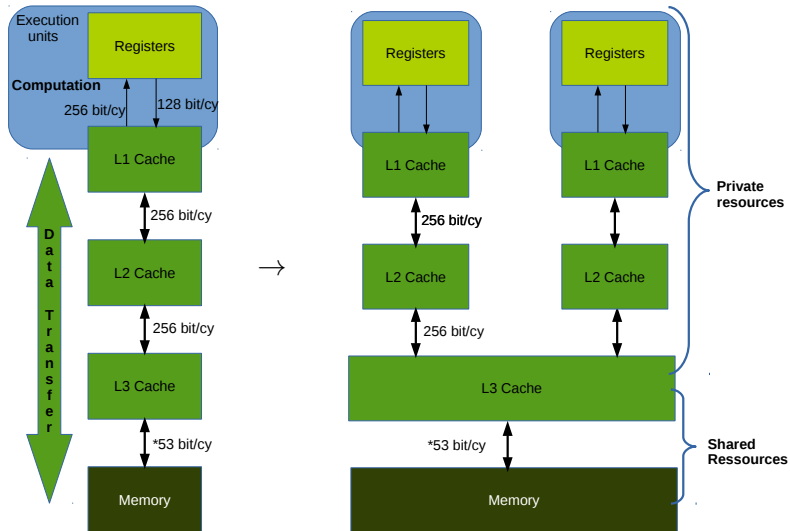
# ECM model vs Roofline model vs measured performance

kernel name	time [cycles / cache line update]	
	prediction ECM	measurement
Pressure correction	80	78
Lagrangian q. update	57	58



modeling error	
Roofline	ECM
30%	3%
70%	2%

# ECM: from one core to full node





Kernel name	Speed up 8-cores SNB		Speed up 4-core HSW	
	Pred.	Meas.	Pred.	Meas.
<b>Lagrange kernels</b>				
Pressure prediction	8	7.45	4	3.5
Pressure correction	2.6	3.0	1.4	1.6
Velocity update	2.8	3.0	1.5	1.5
<b>Remap kernels</b>				
Lagrangian q. update	3.2	3.4	1.6	1.6
Cell centered gradient	8	7.9	4	3.9
MUSCL fluxes	2.3	2.6	1.3	1.4
Cell centered remap	2.5	2.7	1.2	1.6
Node centered gradient	8	7.9	4	3.9
Velocity remap	2.3	2.7	1.5	1.5

## Performance modeling

- Very useful analysis tools for understanding code performance behavior
- Provide qualitative / quantitative information depending on the used model

## Highlighting some bottlenecks in the current solver

- Variable location (node and cell-centered)
- Multi dimensional remap in multiple steps
- Complex geometrical features

## On going works

- Building a new efficient numerical scheme (see F. De Vuyst talk, Thursday 10<sup>th</sup>)
- Performance modeling of this new scheme

Thanks for your attention!